IN THE UNITED STATES PATENT AND TRADEMARK OFFICE
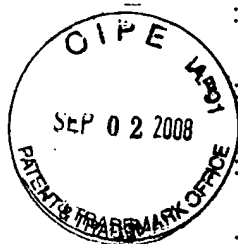
In re application of : **Confirmation No. 6701**

Stefano TUBARO et al. : Attorney Docket No. 2006_0316A

Serial No. 10/571,010 : Group Art Unit 41.92

Filed December 29, 2006 : Examiner Abderrahim Merouan

METHOD FOR DETERMINING
REFLECTIONS IN AN AREA : **Mail Stop: AMENDMENT**

SUBMISSION OF VERIFIED TRANSLATION OF PRIORITY DOCUMENT

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Sir:

In order to perfect the claim of priority under the International Convention to Italian

Patent Application No. MI 2003 A 001719, filed September 8, 2003, a verified English

translation of said Italian Patent Application is submitted herewith.

Respectfully submitted,

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September 2, 2008

DECLARATION

I, Enrico MITTLER, of Residenza Archi 532 – MILANO 2 -

SEGRATE (MI) – Italy, certify that I am conversant in both

Italian and English language, and that the annexed document

in English is a translation of the Italian priority application.

Enrico MITTLER

Dated this 15th day of July 2008

MINISTRY OF PRODUCTIVE ACTIVITIES

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Certification of a copy of documents relative to the patent application for industrial invention

No. MI 2003 A 001719 of 8 September 2003

It is certified that the annexed copy is compliant with the original

documents as filed with the above mentioned patent application, the

data of which are reported on the enclosed filing certificate.

Rome, 5 August 2004

THE OFFICIAL

Giampietro Carlotto
(signature illegible)

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PATENT APPLICATION FOR INDUSTRIAL INVENTION, LATE SUBMISSIONS,
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D. TITLE   class proposed (section/class/underclass)   group/undergroup

"Method for determining reflections in an area"

ADVANCED ACCESSIBILITY TO THE PUBLIC: YES NO X   IF PETITION: DATE   DOCKET N.

E. DESIGNATED INVENTORS   Surname and name   Surname and name
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F. PRIORITY   LATE SUBMISSIONS

State or organization	type	Number	filing date	Encl. (Y/N)	Date	Docket No
1)						
2)						

G. AUTHORIZED CULTURE COLLECTION CENTRE, name

H. SPECIAL NOTES

ENCLOSED DOCUMENTS
No.

							LATE SUBMISSIONS	
							Date	Docket No.
Doc. 1)	1	PROV	No. pages	24	abstract with main drawing, description and claims (1 copy compulsory)		-----	-----
Doc. 2)	1	PROV X	No. sheets	01	drawing (compulsory if cited in description, 1 copy)		-----	-----
Doc. 3)	1	RES			equivalent declaration ~~power of attorney, power or reference to general power of attorney~~		-----	-----
Doc. 4)	0	RES			designation of inventor		-----	-----
Doc. 5)	0	RES			priority documents with Italian translation		compare each priority	
Doc. 6)	0	RES			authorization or deed of assignment		-----	-----
Doc. 7)	0	RES			complete name of applicant		-----	-----

8) payment proof, total Euro 291,80   compulsory

COMPLETED ON 08/09/2003   **APPLICANT(S) SIGNATURE** by POLITECNICO DI MILANO

CONTINUES YES/NO NO   Dr. Ing. Enrico Mittler

A SWORN COPY OF THIS CERTIFICATE IS REQUIRED YES/NO YES

PROVINCIAL DEPARTMENT IND. COMM. ART. OF MILANO   code 15

FILING CERTIFICATE   APPLICATION NUMBER MI2003A 001719   Reg. A

The year TWO THOUSANDTHREE, on the EIGHTH day of the month of SEPTEMBER
the above applicant(s) has(have) filed with me the undersigned the present application, consisting of No. 00 additional sheets for the granting of the above patent.

I. SUNDRY NOTES OF THE RECEIVING OFFICER _____

_____

_____

THE DEPOSITOR   **THE RECEIVING OFFICER**
_____illegible_____   Dept. Stamp   M. CORTONESI

INVENTION ABSTRACT WITH PRINCIPAL DRAWING, DESCRIPTION AND CLAIM
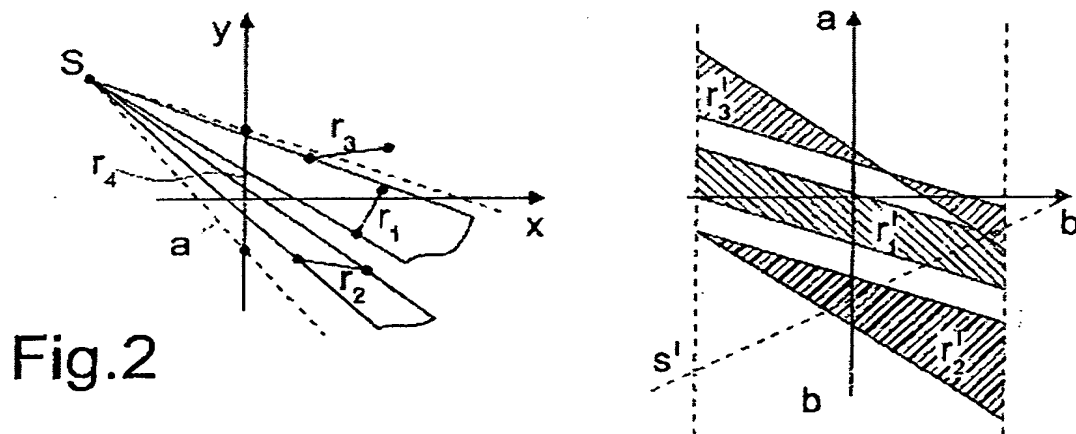
D. TITLE

"Method for determining reflections in an area".

L. ABSTRACT

The present invention refers to a method for determining reflections in complex environments, by means of ray tracing.

For ray tracing it is necessary to determine the region of visibility between at least a first reflector and a second reflector by means of the following phases: representing said first and second reflector in a system of coordinates (x, y, z); said method is characterised in that it further comprises the phases of: carrying out an affine transformation of said system of coordinates (x, y, z); determining the region of visibility of said second reflector in relation to said first reflector as the set of the parameters of the straight lines that link a generic point of said first reflector with a generic point of said second reflector. (Fig. 2).

M. DRAWING

Fig.2

Dr. Ing. Enrico Mittler

DESCRIPTION

of the industrial invention entitled:

"Method for determining reflections in an area".

in the name of: POLITECNICO DI MILANO

* * *

The present invention refers to a method for determining reflections in complex environments, by means of ray tracing.

The rapid tracing of rays, that follow reflection laws similar to geometric optics laws, is a problem of considerable interest in numerous fields of application. In particular, the techniques capable of carrying out this operation find immediate application in the simulation of acoustic reverberations in complex environments, in the photo-realistic rendering of models of three-dimensional scenes, or in the prediction of the electromagnetic propagation of wireless systems in the presence of multiple reflections.

The acoustic or electromagnetic path curves follow paths that, with excellent approximation, meet the geometric optics laws. According to these laws, a ray that has an incidence on a planar reflector with angle α in relation to the normal to the plane is reflected by this in coplanar direction with the plane formed by the incidence vector and the vector normal to the reflector, which results specular in relation to the latter vector (output angle equal to a $-\alpha$). A ray can undergo many reflections by the walls present in the environment, each time diminishing until it becomes of negligible entity. Given a source and a receiver however located in an environment with various reflectors, many paths can exist (in direct or indirect visibility) that connect these points.

There are various approaches to the problem of tracing rays, such as the image sources method, the ray tracing method, and the beam tracing method.

The image sources method calculates the paths corresponding to specular reflections considering the virtual sources obtained through the

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specular reflection of the sources in relation to all the polygons that represent the reflectors of the environment. For each virtual source a specular reflection path can be constructed through the iterative intersection of a rectilinear segment that links source with receiver through the existing reflection planes. The specular reflection paths can be calculated up to an arbitrary order through the recursive generation of virtual sources. The main advantage of the image method is its solidity, as it guarantees that all the required paths are determined up to a pre-assigned reflection order. Against this, the cost of calculating the method grows in exponential proportion of the reflection order and the control of the visibility conditions (to be carried out for each of the virtual sources) results to be of limited complexity only for environments that are not too complex (in fact conditions of occlusion, plausible reflection, etc. have to be considered).

The ray tracing methods are based on the direct tracing of the ray starting from the source until it reaches the receiver o vice versa. Whatever point the ray tracing starts from, these methods typically require the exploration of a finite, but high, number of output directions, to verify that a path exists that complies with the geometric optics laws and that reaches the arrival point after a certain number of reflections. However, this approach often results to be burdensome to calculate as in order to be certain not to excessively undersample the space of the possible directions to explore (and erroneously miss the arrival point), the number of tracing attempts has to be very high.

Beam tracing is capable of preventing this problem through the tracing of compact beams of rays that originated from the same source (real or virtual). This eliminates the risk of missing the arrival point in the tracing operation.

When a beam has incidence on a reflector, all the rays that compose it are reflected according to the geometric optics laws forming a reflected beam that results in coinciding with the specular version (in relation to the

surface of the reflector) of the beam that would be obtained if the reflector was not present.

In general, however, the beam has incidence only in part on the reflector, with the result that only a portion thereof is reflected while the remaining part proceeds undisturbed in its original path. In this case the beam separates into two or more sub-rays in correspondence with the reflector. To carry out beam tracing thus means to construct the tree of the reflections and of their branches that the beam undergoes in its path in space. Clearly, the ray undergoes a natural attenuation that grows with the increase of the length of the path followed. A further attenuation is introduced by the reflection walls. This enables the growth of the tree to be interrupted where the attenuation of the beams reaches a preset threshold.

The reflection tree or beam tree is constructed so as to gather in gerarchic mode all the information needed for the reconstruction of the acoustic paths existing between the source and an arbitrary point. In particular, for each branch point of the tree the position of the source (real or virtual) that generates the reflection to that branch point has to be specified, the geometrical parameters that characterise the extension of the beam, and the information need to identify the reflector - if any - on which the beam will have incidence in following its path. It is assumed, without loss of generality, that the beam has been preliminarily divided into adjoining sub-beams.

Once the beam tree associated to a given position of the source has been constructed, the determination of all the beams that hit a certain point of the space (receiver) is immediate. Going back up the tree it is then possible to derive the direct or reflected paths that link it to the source. This operation results, in fact, in being very rapid as it only requires consultation of the data structure used to memorise the beam tree.

It can be seen however that a movement of the source or even of only one of the reflectors entails the recalculation of the tree, an operation that is

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generally more burdensome than its simple consultation.

In view of the state of the technique described, object of the present invention is to speed up the construction of the beam tree when the source moves, through the separation of the phases of analysis of the visibility and tracing of the beams.

In its first aspect the present invention refers to a method for determining the region of visibility between at least a first reflector and a second reflector comprising the following phases: representing said first and second reflector in a system of coordinates (x, y, z); said method is characterised in that it further comprises the phases of: carrying out a similar transformation of said system of coordinates (x, y, z); determining the region of visibility of said second reflector in relation to said first reflector as the set of the parameters of the straight lines that link a generic point of said first reflector with a generic point of said second reflector.

Preferably, the affine transformation comprises the execution of a rotatory translation of said system of coordinates (x, y, z) so that said first reflector is placed on the plane x = 0.

Preferably, the affine transformation comprises the execution of a scaling down of said system of coordinates (x, y, z) so that said first reflector assumes a preset dimension.

Advantageously, the method comprises a third reflector; and the following phases: determining the region of visibility of said second and third reflector seen from said first reflector; in the case that there are overlapping regions of visibility: tracing a semistraight line in said system of coordinates that has parameters comprised in the overlapping region starting from said first reflector; determining what is the succession of the intersections between said second and third reflector; assigning the overlapping portion of the region of visibility to the reflector having priority succession order; said regions of visibility represent a visibility diagram.

In particular the method is characterised in that it represents said first

reflector and second reflector in a system of coordinates (x, y) by means of segments; carrying out an affine transformation of said system of coordinates (x, y) capable of bringing said first reflector to assuming coordinates of the extremes in the points (0, m) and (0, n) with $m < n$; representing said second reflector by means of the following system of equations $x = e\,t + f$, $y = g\,t + h$, with $0 \leq t \leq 1$; representing a generic straight line by means of the parameters a, b of the equation $y = a\,x + b$; determining the region of visibility by determining all the straight lines that pass through a generic point of the first and of the second reflector combining the previous equations and obtaining the following system $g\,t + h = a\,(e\,t + f) + b$, with $0 \leq t \leq 1$ and with $m \leq b \leq n$.

In its second aspect the present invention refers to a method for determining a beam tree of the beams of the rays on a plurality of reflectors that comprises the phases of prior determination of the set of the regions of visibility from each reflector in accordance with the previously described method.

Advantageously, the method for determining a beam tree of the beams of the rays on a plurality of reflectors comprises the phases of prior determination of the visibility diagram in accordance with the previously described method; positioning a source in a system of coordinates (x, y); determining the areas of the reflectors illuminated by said source in said system of coordinates (x, y); memorising the coordinates of said areas of the reflectors illuminated by said source; representing a virtual source for each reflector illuminated; applying said affine transformation of said system of coordinates (x, y) to said virtual source and to said illuminated region; said transformed illuminated region is represented by means of a segment of extremes $(0, b_0)$ and $(0, b_1)$; representing said transformed virtual source in the space of the parameters (a, b) by means of the equation $y = a\,x + b$, and the illuminated region by means of the disequation $b_0 \leq b \leq b_1$; the system of equations $y = a\,x + b$ and $b_0 \leq b \leq b_1$ represents a segment of illumination in

the space of the parameters (a, b); intersecting said segment of illumination with said visibility diagram obtaining sub-segments and thus sub-intervals of the interval $b_0 \leq b \leq b_1$; said sub-intervals will represent portions of the illuminated region and each one will illuminate a new reflector.

In its third aspect the present invention refers to a program for computer comprising a program code that carries out all the phases of the method for determining the region of visibility between at least a first reflector and/or of the method for determining a beam tree when the program is carried out on a computer.

In its fourth aspect the present invention refers to a program for computer recorded on a support that can be used by a computer for controlling the execution of all the phases of the method for determining the region of visibility between at least a first reflector and/or of the method for determining a beam tree.

The present invention permits to carry out the bulkiest calculation operations of assessment of the visibility in a preliminary phase that considers only the reciprocal positions of the reflectors, independently from the position of the source. The visibility is in fact redefined in a suitable parametric space, where the information for its assessment can be organised under the form of diagrams. The construction of the beam tree is then carried out each time the source moves, using the precalculated information of visibility.

The characteristics and advantages of the present invention will appear evident from the following detailed description of an embodiment thereof, illustrated as non-limiting example in the enclosed drawings, in which:

Figures 1a, 1b and 1c show an example of rotatory-translation, of normalization and transformation from a space with coordinates (x, y) to a space with parameters (a, b);

Figures 2a and 2b show an example of construction of the visibility diagram;

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Figures 3a and 3b show an example of construction of a level of the beam tree.

As the method herein proposed refers to the tracing of paths that follow the geometric optics laws, phenomenon such as diffraction will not be considered, which occurs when the dimensions of the reflectors become comparable with the wavelength of the wave that propagates in the environment. This assumption, even though correct in the case of high frequency electromagnetic waves (light or microwaves), results only approximately satisfied in the case of the propagation of acoustic waves, and in fact it has been calculated that these models are valid for simulations above 150Hz (corresponding to the wavelength of approximately 2 metres, a length that starts to be comparable with the dimensions of the walls of a living or working environment). In addition, even though it is true that sufficiently wide walls reflect in an almost specular manner, rough edges of rigid reflectors tend to generate a diffraction that is not negligible. In particular, small objects (a vase, a cup, etc.) tend to have significant effects on the acoustic field for sounds whose frequency is above 4kHz. These objects, however, are not generally considered in the modellation of acoustic environments.

For simplicity of description, hereinafter the phenomenon of the transmission through the walls will also be neglected. Hereinafter it will be illustrated how it is possible to take account of it through simple modifications of the method illustrated herein.

The entities that we shall now consider are the sources, the receiver and the reflectors.

It is assumed that the sources and receivers are pointed elements, while the reflection walls are described by segments in the two-dimensional case and by portions of polygonal planes, for example triangles, in the three-dimensional case. Each wall of reflection defines two reflectors, one for each side. This distinction, as will be seen, is substantial in that it has

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consequences on the choice of parameters that characterise the visibility.

We can say that a source "illuminates" a point if there is a direct path that links them. With the term "virtual source" we intend the specular reflection of a real source in relation to a reflecting wall. In addition that region of a reflector that is directly illuminated by the source considered is defined "active". The active portion of a reflector can be composed of one or more active segments (also disconnected because of possible partial occlusions). Each of the active segments generates a new reflected beam.

Identifying the reflectors present in the environment with a whole index i, the visibility is defined as a function that associates the index of the visible reflector to a view point and to a view direction. This function is thus defined in the space of the parameters that characterise view point and direction, and is constant at times. The visibility from a reflector is thus defined as the visibility function from all points of the reflector itself.

The assessment of the visibility of an environment, that is of a set of reflectors, consists in the construction of the visibility functions associated to all the reflectors of the environment. As it is assumed that the reflecting walls reflect on both sides, the visibility of an environment composed of M walls will be characterised by 2M visibility functions.

The preliminary assessment procedure of the visibility of the environment through the construction of the visibility by the generic reflector is now illustrated. To be able to conveniently define the space of the parameters on which the visibility function assumes values, it is preferable to carry out a affine transformation of the geometric space that leads the reflector to assume preselected position, orientation and, finally, shape.

As previously illustrated, the visibility function assumes values on the space of the parameters that characterise a view point and direction. If the point lies on the reflector, the space of the parameters will be four-dimensional in the case of three-dimensional environments, or two-

dimensional in the case of two-dimensional environments. We assume that the geometric space has been preliminarily submitted to affine transformation that brings the reflector to lie on plane x = 0, with reflecting face turned towards the semi-axis x ≥ 0. A convenient parametizing for view point and direction is thus given by the system of equations

$$y = a\,x + b$$

$$z = c\,x + d$$

where the couple of parameters (b, d) identifies the view point on the plane (y, z) of the reflector, while the couple of parameters (a, c) defines the view direction. In the case of two-dimensional environments only the first of the two equations has to be considered, and the parameters a and b will identify the view direction and point respectively.

For reasons of simplicity of description, we will limit ourselves for the moment to consider only the case of two-dimensional environments. In this case, the affine transformation of the geometric space can be defined simply as a rotatory-translation with scaling down that transforms the reflector in the segment that links the points(0, -1) and (0, 1), with reflection face turned towards the semi-axis x ≥0. This enables the space of the parameters at the interval −1 ≤ b ≤ 1 to be limited. The visibility function will thus be a constant function at times in the space (a, b), where the values identify the visible reflectors.

We will consider two reflectors r_0 and r_1, having as references respectively q_0, p_0 and q_1, p_1, located casually in a space with coordinates (x, y), as shown in Figure 1a.

We roto-translate the reflectors placing the reflector r_0 in question to coincide with the vertical axis y (x=0). We normalize, again for practicality, the reflectors, that is the segment having as references p'_0 and q'_0 of coordinates (0, 1) and (0, -1) has been chosen as representation of the reflector r_0. Thus a representation of the reflectors as shown in Figure 1b is obtained. Representing the reflectors in the space of the parameters (a, b) the

diagram in Figure 1c is obtained.

In the space of the parameters (a, b), in Figure 1c, the space o comprised between the four straight lines p"₀, p"₁, q"₀, q"₁ represents the visibility of r'₁ from r'₀.

We define the region of visibility of a generic reflector in relation to the reflector of reference as that region of the space of the parameters (a, b) to which view points and directions from which that reflector is visible correspond. As occlusions by other reflectors can occur, this region can result empty, or composed of one or more convex polygons. In each region of visibility the visibility function will obviously result to be constant. Vice versa, the region of visibility associated to the umpteenth reflector, corresponds to the region in which the function assumes value i. It is in addition useful to define the region of potential visibility of a reflector in comparison to the reference reflector, like the region of visibility calculated in absence of all the other reflectors. The effective region of visibility will be justly contained in the region of potential visibility, as the regions of potential visibility of all the reflectors can overlap.

The construction of the visibility function associated to a reference reflector is carried out in two successive phases: first the regions of potential visibility of the single reflectors are assessed, then the regions of effective visibility are assessed through determinations of the reciprocal occlusions.

For determining the region of potential visibility of the generic reflector compared to the reference reflector, the parameters of all the straight lines that start from any point of the reference reflector (in positive direction) and have incidence on the reflecting side of the reflector considered at any point are determined. To this object, first of all the generic reflector is defined with the couple of equations:

$$x = e\,t + f$$

$$y = g\,t + h$$

where t is a parameter comprised between 0 and 1. Replacing these

expressions in the equation $y = ax + b$ we obtain a region in the space of the parameters characterised by:

$$g\,t + h = a\,(e\,t + f) + b, \quad 0 \le t \le 1$$

$$-1 \le b \le 1$$

This region results to be thus the intersection between a beam of semi-straight lines and the reference strip $-1 \le b \le 1$.

When the areas of potential visibility of two reflectors overlap each other in the space of the parameters, it means that a reflector partially blocks the other in relation to the generic view point on the reference reflector. The second phase of the procedure for assessing the visibility function consists in assigning the correct index to the regions in which the regions of potential visibility overlap each other. This operation can be carried out in various ways. The most simple method consists of determining which reflector occludes all the others by means of tracing a sample view ray chosen inside the overlapping region. At the end of this operation we obtain a partitioning of the space of the parameters in areas of effective visibility, to each of which is associated at the most a visible reflector. We will call this geometric representation of the visibility function, visibility diagram.

Now we consider four reflectors r_1-r_4, and we want to determine the visibility diagram of the reflector r_4. Thus, we roto-translate and normalize the reflector r_4 and we obtain a representation in space with coordinate (x, y) as shown in Figure 2a, and in the space of the parameters (a, b) as shown in Figure 2b. We also consider a source S represented in the space of the parameters (a, b) with the straight line S'. It can be seen that in Figure 1a, the reflector r_3 partially occludes the reflector r_1. An occlusion in the space of the parameters (a, b) is represented by an overlapping of areas. Analysing the slopes of the straight lines that enclose the overlapped areas it is possible to determine in the correct way the relative visibility. In particular, the greater slope dominates the minor slope.

This operation of construction of the functions (diagrams) of visibility is

carried out on all the reflectors present in the scene (two per wall) in a preliminary analysis phase.

At this point the real tracing of the beams for the construction of the beam tree can be started, an operation that is possible when the position of the source is known. As already partially anticipated, each branch point of the beam tree is associated to a beam, and is characterised by the following information: position of the real or virtual source, index and illuminated portion of the reflector on which the beam has incidence.

The present method enables in particular the construction of the upper branching of the beam tree at the first level to be sped up. The construction of the branching of the root of the tree (primary beams) can come about, as in the classic method, tracing a beam at 360 degrees from the source and verifying the occlusions in the geometric space.

The beam tracing procedure comes about in recursive mode. After having divided the beam emitted by the real source into primary beams, each associated to a reflector in visibility, they are reflected and the recursive determination of the successive branching is made.

Given a beam reflected by the umpteenth reflector, the information of the visibility diagram associated to it is used to determine the subdivision of the beam into sub-beams, one for each reflector in visibility.

In practice, the procedure is as follows: first of all the transformation used to bring the reflector associated to the beam in canonic reference position is applied to the virtual source, that brings it to lie on the left of the reflector. At this point the interval $b_0 \leq b \leq b_1$ that characterises the portion of beam that actually illuminates the reflector is determined. Then the representation of the beam on the dominium of the visibility diagram is identified.

Replacing the point identified by the virtual source in the equation $y = ax + b$ the equation of a straight line in the space of the parameters (a, b) is obtained, which together with the condition $b_0 \leq b \leq b_1$ represents a

segment. Intersecting this segment with the areas that compose the visibility diagram of the reflector a series of sub-segments of the original segment is obtained, each of which represents in the geometric space a new beam that will have incidence on a single reflector. Using this information a new level of the tree will be created.

Figure 3 refers to the construction of a level of the tree, based on the reflections of the reflector r_4 of Figure 2. Positioning the straight line S' in the space of the parameters (a, b), this intersects the reference area (-1 $\leq$ b $\leq$ 1) in 5 sub-rays numbered from 1 to 5. The rays 1 and 3 are rays that are not reflected and proceed without limits, while the rays 2, 3 and 5 are reflected by the reflectors r_2, r_1 and r_3 respectively. The information relating to the position of the source that generates the reflection to that branch node, the geometric parameters that characterise the extension of the beam, and the information needed to identify the eventual reflector on which the beam will have incidence in continuing its path are associated to each branch node. In this manner the tree is created, and the process is repeated for each reflection of the rays, until the number of reflections reaches a preset number or the energy associate to the ray becomes negligible.

The information present in the beam tree enable the generation of a filter (FIR) on the basis of which paths reach the location of the listener. This updating is rapid and can be carried out frequently.

Through this process it is possible to obtain for each path its own direction of arrival (DOA), the length of the path and the list of the reflectors with which it has interacted along the path. This phase requires all the branches and the leaves of the tree to have been visited and has to be controlled if the receiver is present in the beam being considered. If the receiver is present, the direction of arrival (DOA) of the ray and the length of the path are calculated. Therefore, passing along the whole tree to the root the list of reflectors met is obtained.

Since it is impossible to produce a flow for each DOA, angular intervals

have been grouped together to generate a limited number of audio flow, one per interval. Each of these angular intervals will be attributed to separate delay lines of the filter FIR, that are calculated taking into account all the paths and the relative attenuations.

The filter calculated in this manner is capable, given an anechoic source (that is a source recorded in a room without reverberation), of obtaining the result of listening to that sound in a room represented by the geometry of the reflectors.

The method allows immediate extension to the three-dimensional case. Also in the 3D case it is possible to carry out an affine transformation of the geometric space that enables the scansion interval to be preset, and to simplify the representation of the visibility function. As we will see hereinafter, without losing generalities, we will consider a geometric transformation that brings the plane on which the reflector lies to coincide with the plane x=0 and brings the polygon to assume a preset canonic form.

As already previously mentioned, the space of the parameters of the straight lines in three-dimensional environments is four-dimensional. Downstream from the geometric transformation of the polygonal reference reflector, we can express the generic straight line of the space 3D with the system of equations $y = a x + b$ and $z = c x + d$, in which (a, b, c, d) identify the space of the parameters. In this space the representation of the potential visibility is still given by set of the straight lines that have incidence on both the reflectors considered, which this time is a closed portion of the four dimensions space. For practicality, it is also possible to limit before the category of polygons that interest. A particularly advantageous choice is that of the triangles: this transformation does not remove generalities from the method, as it is always possible to represent a complex plane polygon by means of its triangulation; in addition it is quite frequent, also in Computer Graphics, that the surfaces in the three-dimensional space are modelled with triangle nets. In the case of two triangular reflectors, the region of potential

visibility can be expressed in the form of 6 disequation system, needed for the set of the straight lines having incidence on both the triangles. For example, expressing the generic reflector by means of the system of equations:

$$x = a_x t + b_x s + c_x$$
$$y = a_y t + b_y s + c_y$$
$$z = a_z t + b_z s + c_z$$
$$t \geq 0$$
$$s \geq 0$$
$$t + s \leq 1$$

The system that represents the generic straight line passing through the reference reflector, previously normalized by an affine transformation that makes its three vertexes coincide with the three points (0, 0, 0), (0, 1, 0) and (0, 0, 1), is represented by the system:

$$y = a\,x + b$$
$$z = c\,x + d$$
$$b \geq 0$$
$$d \geq 0$$
$$b + d \leq 1$$

Replacing the first three equations of the first system, in the equations of the second system we obtain two equations, from which we can derive the parameters s and t in function of the variables a, b, c, d. Replacing the values of the parameters s and t in the disequations of the first system, and adding the disequations of the second system we obtain a system of 6 disequations in the parameters a, b, c, d, that delimit the area of potential visibility between the two reflectors.

In a similar manner to the two-dimensional case it is possible to decide the order of occlusion between overlapped regions of potential visibility, and thus it is possible to construct for each reflector a visibility diagram represented by a subdivision of the space of the parameters in regions of

effective visibility, each of which is associated at the most to a reflector.

The representation of the source and of the illuminated area is given by describing all the straight lines that intersect it with a limited beam, obtaining a system of two equations and some disequations in the four unknown quantities, that identifies a portion of a two-dimensional subspace. The subdivision of the beam will come about in this case intersecting the areas of the visibility diagram associated to the reflector that has generated the beam with the portion of plane that represents the beam reflected in the space (a, b, c, d). The method for the construction of the tree remains thus completely similar to the two-dimensional case.

It can be noted that the choice of the transformation on the plane $x = 0$, both in the two-dimensional case and in the three-dimensional case, is not binding, but it has been introduced with the sole object of simplifying the exposition, placing the equations of the straight lines in an easier form.

The method for determining the visibility between reflectors and the method for determining a beam tree, herein described, can be transcribed in a program, in a well-known manner by a technician of the sector, and can be memorised on any type of memory or support (floppy, CD) and/or can be made to be carried out by a computer.

CLAIMS

1. Method for determining the region of visibility between at least a first reflector and a second reflector comprising the following phases:

representing said first and second reflector in a system of coordinates (x, y, z);

said method is characterised in that it comprises the further phases of:

carrying out an affine transformation of said system of coordinates (x, y, z);

determining the region of visibility of said second reflector in relation to said first reflector as the set of the parameters of the straight lines that link a generic point of said first reflector with a generic point of said second reflector.

2. Method in accordance with claim 1 characterised in that said affine transformation comprises the execution of a rotatory-translation of said system of coordinates (x, y, z) so that said first reflector is placed on the plane x = 0.

3. Method in accordance with claim 1 characterised in that said affine transformation comprises the execution of a scaling down of said system of coordinates (x, y, z) so that said first reflector assumes preset dimension.

4. Method in accordance with claim 1 characterised in that it comprises a third reflector; and the following phases:

determining the region of visibility of said second and third reflector seen from said first reflector;

in the case that there are overlapped regions of visibility tracing a semistraight line in said system of coordinates whose parameters are comprised in the overlapping region starting from said first reflector;

determining what is the succession of the intersections between said second and third reflector;

assigning the portion of overlapped region of the region of visibility to the reflector having priority succession order;

said regions of visibility represent a visibility diagram.

5. Method in accordance with claim 1 characerised by:

representing said first reflector and second reflector in a system of coordinates (x, y) by means of segments;

executing an affine transformation of said system of coordinates (x, y) capable of leading said first reflector to assume coordinates of the extremes in the points(0, m) and (0, n) with m < n;

representing said second reflector by means of the following system of equations

x = and t + f

y = g t + h

with $0 \leq t \leq 1$

representing a generic straight line by means of the parameters a, b of the equation y = a x + b;

determining the region of visibility determining all the straight lines that pass through a generic point of the first and of the second reflector combining the previous equations and obtaining the following system

g t + h = a (e t + f) + b

with $0 \leq t \leq 1$ and with $m \leq b \leq n$.

6. Method for determining a beam tree of beams of rays on a plurality of reflectors comprising the phases of previously determining the set of the region of visibility from each reflector in accordance with claim 1.

7. Method for determining a beam tree of beams of rays on a plurality of reflectors comprising the phases of previously determining the visibility diagram in accordance with the previous claims;

positioning a source in a system of coordinates (x, y);

determining in said system of coordinates (x, y) the areas of the reflectors illuminated by said source;

memorizing the coordinates of said areas of the reflectors illuminated by said source;

representing a virtual source for each reflector illuminated;

applying said affine transformation of said system of coordinates (x, y) to said virtual source and to said illuminated region;

said illuminated transformed region is represented by means of a segment of extremes $(0, b_0)$ and $(0, b_1)$;

representing said virtual source transformed in the space of the parameters (a, b) by means of the equation $y = a x + b$, and the illuminated region by means of the disequation $b_0 \leq b \leq b_1$;

the system of equations $y = a x + b$ and $b_0 \leq b \leq b_1$ represents a segment of illumination in the space of the parameters (a, b);

intersecting said segment of illumination with said visibility diagram obtaining sub-segments and thus sub-intervals of the interval $b_0 \leq b \leq b_1$;

said sub-intervals will represent portions of the illuminated region that will each illuminate a new reflector.

8. Program for computer comprising a program code that carries out all the phases of any previous claim when said program is executed on said computer.

9. Program for computer recorded on a support that can be used by said computer for controlling the execution of all the phases of any previous claim.

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